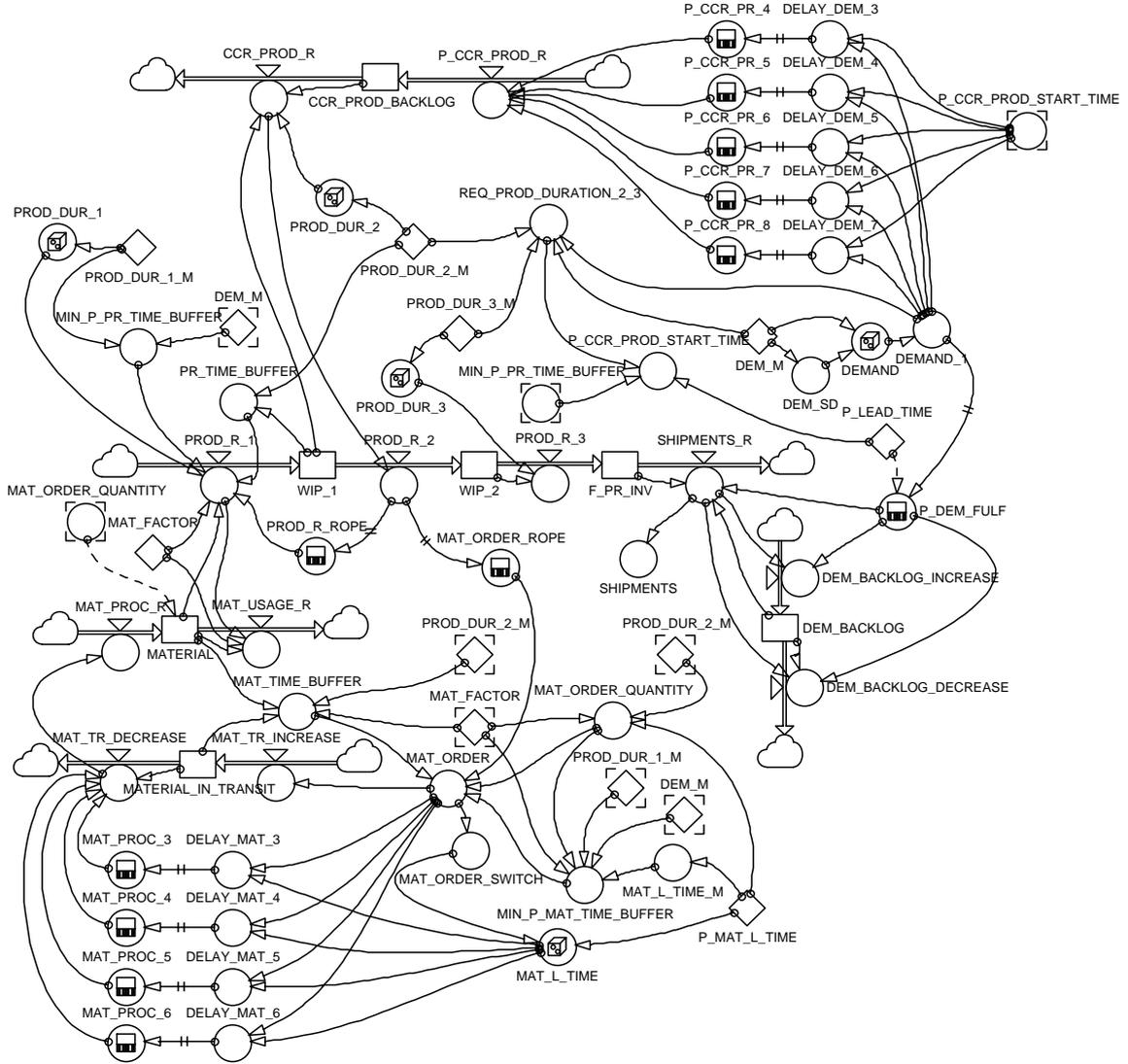


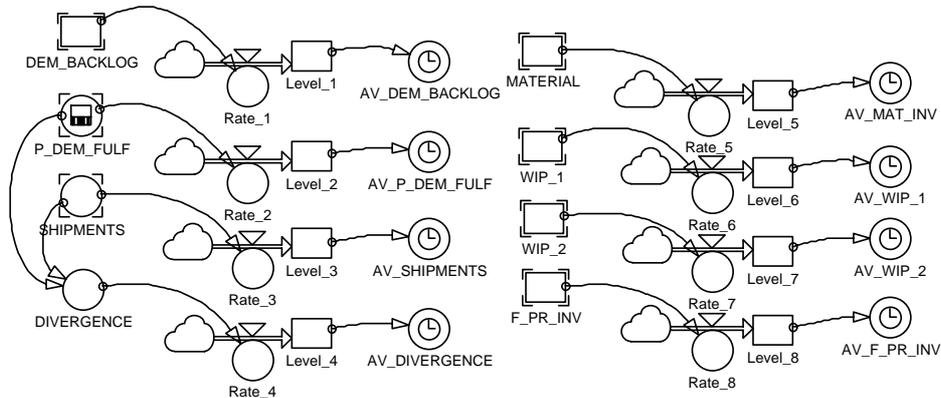
# Stock-flow Diagrams and Equations Omitted from the Main Text due to File Size Limit

## A. DBR approach

### A.1 Stock-flow Diagram for Scheduling and Production Sector



### A.2 Stock-flow Diagram for Controlling Sector



### A.3 Equations

init CCR\_PROD\_BACKLOG = 0  
flow CCR\_PROD\_BACKLOG =  $-dt*CCR\_PROD\_R$   
 $+dt*P\_CCR\_PROD\_R$   
doc CCR\_PROD\_BACKLOG = This is what we have to produce at the CCR operation of the shop, in order the demand to be fulfilled at its planned lead time, considering: (i) what we want to produce at the CCR operation at the current time interval and (ii) what we wanted to produce at the CCR operation at the previous time interval and we couldn't produce due to the lack of capacity of the CCR operation.  
unit CCR\_PROD\_BACKLOG = ITEMS

init DEM\_BACKLOG = 0  
flow DEM\_BACKLOG =  $-dt*DEM\_BACKLOG\_DECREASE$   
 $+dt*DEM\_BACKLOG\_INCREASE$   
doc DEM\_BACKLOG = This is the demand, whose fulfillment is going to be delayed (i.e. it is going to be satisfied more than 10 days after its release).  
unit DEM\_BACKLOG = ITEMS

init F\_PR\_INV = 0  
flow F\_PR\_INV =  $-dt*SHIPMENTS\_R+dt*PROD\_R\_3$   
doc F\_PR\_INV = This is the inventory of the finished product, which is available after the end operation of the shop.  
unit F\_PR\_INV = ITEMS

init Level\_1 = 0  
flow Level\_1 =  $+dt*Rate\_1$   
doc Level\_1 = This level is used to calculate the average value of the demand backlog (AV\_DEM\_BACKLOG).  
unit Level\_1 = ITEMS\*days

init Level\_2 = 0  
flow Level\_2 =  $+dt*Rate\_2$   
doc Level\_2 = This level is used to calculate the average value of the planned demand fulfillment (AV\_P\_DEM\_FULF).  
unit Level\_2 = ITEMS

init Level\_3 = 0  
flow Level\_3 =  $+dt*Rate\_3$   
doc Level\_3 = This level is used to calculate the average value of the shipments (AV\_SHIPMENTS).  
unit Level\_3 = ITEMS

init Level\_4 = 0  
flow Level\_4 =  $+dt*Rate\_4$   
doc Level\_4 = This level is used to calculate the average value of the divergence (AV\_DIVERGENCE).  
unit Level\_4 = ITEMS

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init Level_5 = 0
flow Level_5 = +dt*Rate_5
doc Level_5 = This level is used to calculate the average value of the raw material
inventory (AV_MAT_INV).
unit Level_5 = Kg*DAYS

init Level_6 = 0
flow Level_6 = +dt*Rate_6
doc Level_6 = This level is used to calculate the average value of the inventory after
the first operation of the flow shop (AV_WIP_1).
unit Level_6 = ITEMS*DAYS

init Level_7 = 0
flow Level_7 = +dt*Rate_7
doc Level_7 = This level is used to calculate the average value of the inventory after
the second operation of the flow shop (AV_WIP_2).
unit Level_7 = ITEMS*DAYS

init Level_8 = 0
flow Level_8 = +dt*Rate_8
doc Level_8 = This level is used to calculate the average value of the finished product
inventory of the flow shop (AV_F_PR_INV).
unit Level_8 = ITEMS*DAYS

init MATERIAL = 2*MAT_ORDER_QUANTITY
flow MATERIAL = -dt*MAT_USAGE_R+dt*MAT_PROC_R
doc MATERIAL = This is the current level of material inventory on hand. Its initial
value is set equal to 2 times the quantity of the minimum material order.
unit MATERIAL = Kg

init MATERIAL_IN_TRANSIT = 0
flow MATERIAL_IN_TRANSIT = -dt*MAT_TR_DECREASE
+dt*MAT_TR_INCREASE
doc MATERIAL_IN_TRANSIT = This is the current level of material inventory in
transit; i.e. the material inventory that has been ordered and it is expected to be
delivered at the shop later. Its initial value is set equal to zero.
unit MATERIAL_IN_TRANSIT = Kg

init WIP_1 = 0
flow WIP_1 = +dt*PROD_R_1-dt*PROD_R_2
doc WIP_1 = This is the inventory available before the CCR operation of the shop.
unit WIP_1 = ITEMS

init WIP_2 = 0
flow WIP_2 = -dt*PROD_R_3+dt*PROD_R_2
doc WIP_2 = This is the inventory available after the CCR operation of the shop.
unit WIP_2 = ITEMS

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aux  $CCR\_PROD\_R = \min(CCR\_PROD\_BACKLOG/TIMESTEP, 1/PROD\_DUR\_2, WIP\_1/TIMESTEP)$   
 doc CCR\_PROD\_R = This is what we produce at the shop's CCR operation considering what we have to produce (CCR\_PROD\_BACKLOG), the current capacity of the CCR operation (1/PROD\_DUR\_2) and the availability of work in process before the CCR operation (WIP\_1).  
 unit CCR\_PROD\_R = ITEMS/DAY

aux  $DEM\_BACKLOG\_DECREASE = \min(\max(SHIPMENTS\_R - P\_DEM\_FULF/TIMESTEP, 0), DEM\_BACKLOG/TIMESTEP)$   
 doc DEM\_BACKLOG\_DECREASE = This is the demand fulfillment with delay at the current time interval; i.e. it is the demand satisfied later than 10 days (P\_L\_TIME) after its release.  
 unit DEM\_BACKLOG\_DECREASE = ITEMS/DAY

aux  $DEM\_BACKLOG\_INCREASE = \max(P\_DEM\_FULF/TIMESTEP - SHIPMENTS\_R, 0)$   
 doc DEM\_BACKLOG\_INCREASE = This is the invalid demand fulfillment at the current time interval; i.e. it is the demand that although has to be satisfied at the current time interval (10 days after its release), it is impossible to be satisfied on time.  
 unit DEM\_BACKLOG\_INCREASE = ITEMS/DAY

aux  $MAT\_PROC\_R = MAT\_TR\_DECREASE$   
 doc MAT\_PROC\_R = This is the rate of the raw material procurement received; i.e. the raw material delivery at the current time interval. It is set equal to the material in transit decrease.  
 unit MAT\_PROC\_R = kg/DAY

aux  $MAT\_TR\_DECREASE = \min(MAT\_PROC\_3 + MAT\_PROC\_4 + MAT\_PROC\_5 + MAT\_PROC\_6, MATERIAL\_IN\_TRANSIT)/TIMESTEP$   
 doc MAT\_TR\_DECREASE = This is the rate of the raw material received; i.e. the raw material delivery at the current time interval.  
 unit MAT\_TR\_DECREASE = kg/DAY

aux  $MAT\_TR\_INCREASE = MAT\_ORDER/TIMESTEP$   
 doc MAT\_TR\_INCREASE = This is the raw material quantity ordered at the current time interval.  
 unit MAT\_TR\_INCREASE = kg/DAY

aux  $MAT\_USAGE\_R = \min(PROD\_R\_1 * MAT\_FACTOR, MATERIAL/TIMESTEP)$   
 doc MAT\_USAGE\_R = This is the rate of the raw material usage by the production at the gateway operation of the shop (PROD\_R\_1).  
 unit MAT\_USAGE\_R = kg/DAY

aux  $P\_CCR\_PROD\_R = (P\_CCR\_PR\_4 + P\_CCR\_PR\_5 + P\_CCR\_PR\_6 + P\_CCR\_PR\_7 + P\_CCR\_PR\_8) / TIMESTEP$   
 doc P\_CCR\_PROD\_R = This is the Planned CCR Production Rate, i.e. it is what we want to produce at the shop's CCR operation, in order the demand to be fulfilled at its planned lead time.  
 unit  $P\_CCR\_PROD\_R = \text{ITEMS/DAY}$

aux  $PROD\_R\_1 = \text{MIN}(\text{IF}(\text{PR\_TIME\_BUFFER} \geq \text{MIN\_P\_PR\_TIME\_BUFFER}, \text{MIN}(\text{PROD\_R\_ROPE}, 1/\text{PROD\_DUR\_1}), 1/\text{PROD\_DUR\_1}), \text{MATERIAL}/\text{MAT\_FACTOR}/\text{TIMESTEP})$   
 doc PROD\_R\_1 = This is what we produce at the gateway operation of the shop according to the DBR logic and Real Time methodology; i.e. the production rate at the gateway operation of the shop is equal with the production rate of the CCR at the time interval before 4 time steps, considering its production capacity and the availability of raw material required. Besides, if the current production time buffer is less than the minimum one, the production rate at the gateway operation of the shop is equal with its production capacity considering the availability of raw material required.  
 unit  $PROD\_R\_1 = \text{ITEMS/DAY}$

aux  $PROD\_R\_2 = CCR\_PROD\_R$   
 doc PROD\_R\_2 = This is what we produce at the shop's CCR operation.  
 unit  $PROD\_R\_2 = \text{ITEMS/DAY}$

aux  $PROD\_R\_3 = \text{MIN}(1/\text{PROD\_DUR\_3}, \text{WIP\_2}/\text{TIMESTEP})$   
 doc PROD\_R\_3 = This is what we produce at the third operation of the shop.  
 unit  $PROD\_R\_3 = \text{ITEMS/DAY}$

aux  $Rate\_1 = \text{DEM\_BACKLOG}$   
 doc Rate\_1 = This rate is used to calculate the average value of the demand backlog (AV\_DEM\_BACKLOG).  
 unit  $Rate\_1 = \text{ITEMS}$

aux  $Rate\_2 = P\_DEM\_FULF/\text{TIMESTEP}$   
 doc Rate\_2 = This rate is used to calculate the average value of the planned demand fulfillment (AV\_P\_DEM\_FULF).  
 unit  $Rate\_2 = \text{ITEMS/DAY}$

aux  $Rate\_3 = \text{SHIPMENTS}/\text{TIMESTEP}$   
 doc Rate\_3 = This rate is used to calculate the average value of the shipments (AV\_SHIPMENTS).  
 unit  $Rate\_3 = \text{ITEMS/DAY}$

aux  $Rate\_4 = \text{DIVERGENCE}/\text{TIMESTEP}$   
 doc Rate\_4 = This rate is used to calculate the average value of the divergence (AV\_DIVERGENCE).  
 unit  $Rate\_4 = \text{ITEMS/DAY}$

aux Rate\_5 = MATERIAL  
doc Rate\_5 = This rate is used to calculate the average value of the raw material inventory (AV\_MAT\_INV).  
unit Rate\_5 = Kg

aux Rate\_6 = WIP\_1  
doc Rate\_6 = This rate is used to calculate the average value of the inventory after the first operation of the flow shop (AV\_WIP\_1).  
unit Rate\_6 = ITEMS

aux Rate\_7 = WIP\_2  
doc Rate\_7 = This rate is used to calculate the average value of the inventory after the second operation of the flow shop (AV\_WIP\_2).  
unit Rate\_7 = ITEMS

aux Rate\_8 = F\_PR\_INV  
doc Rate\_8 = This rate is used to calculate the average value of the finished product inventory of the flow shop (AV\_F\_PR\_INV).  
unit Rate\_8 = ITEMS

aux SHIPMENTS\_R = MIN(P\_DEM\_FULF+DEM\_BACKLOG,F\_PR\_INV)  
/TIMESTEP  
doc SHIPMENTS\_R = This is the rate of demand shipments.  
unit SHIPMENTS\_R = ITEMS/DAY

aux AV\_DEM\_BACKLOG = Level\_1 DIVZ0 TIME  
doc AV\_DEM\_BACKLOG = This is the average value of the demand backlog (DEM\_BACKLOG) from the simulation start up to the current time interval.  
unit AV\_DEM\_BACKLOG = ITEMS

aux AV\_DIVERGENCE = Level\_4 DIVZ0 TIME  
doc AV\_DIVERGENCE = This is the average value of the DIVERGENCE from the simulation start up to the current time interval.  
unit AV\_DIVERGENCE = ITEMS/DAY

aux AV\_F\_PR\_INV = Level\_8 DIVZ0 TIME  
doc AV\_F\_PR\_INV = This is the average value of the finished product inventory (F\_PR\_INV) from the simulation start up to the current time interval.  
unit AV\_F\_PR\_INV = ITEMS

aux AV\_MAT\_INV = Level\_5 DIVZ0 TIME  
doc AV\_MAT\_INV = This is the average value of the raw material inventory on hand (MAT\_INV) from the simulation start up to the current time interval.  
unit AV\_MAT\_INV = Kg

aux AV\_P\_DEM\_FULF = Level\_2 DIVZ0 TIME  
doc AV\_P\_DEM\_FULF = This is the average value of the planned demand fulfillment (P\_DEM\_FULF) from the simulation start up to the current time interval.

unit AV\_P\_DEM\_FULF = ITEMS/DAY

aux AV\_SHIPMENTS = Level\_3 DIVZ0 TIME  
doc AV\_SHIPMENTS = This is the average value of the SHIPMENTS from the simulation start up to the current time interval.  
unit AV\_SHIPMENTS = ITEMS/DAY

aux AV\_WIP\_1 = Level\_6 DIVZ0 TIME  
doc AV\_WIP\_1 = This is the average value of the inventory after the first operation of the shop (WIP\_1) from the simulation start up to the current time interval.  
unit AV\_WIP\_1 = ITEMS

aux AV\_WIP\_2 = Level\_7 DIVZ0 TIME  
doc AV\_WIP\_2 = This is the average value of the inventory after the second operation of the shop (WIP\_2) from the simulation start up to the current time interval.  
unit AV\_WIP\_2 = ITEMS

aux DELAY\_DEM\_3 = DEMAND\_1\*IF(P\_CCR\_PROD\_START\_TIME<=5,1,0)  
doc DELAY\_DEM\_3 = This is the DEMAND whose production -in order to be dispatched on time- has P\_CCR\_PROD\_START\_TIME less than 5. The production of this demand has to start at the shop's CCR operation (i.e. it has to become part of the rate CCR\_PROD\_R) at the start of the 4th day after the current time interval. Therefore, it has to be added at the rate P\_CCR\_PROD\_R 3 days after the current time interval.  
unit DELAY\_DEM\_3 = ITEMS

aux DELAY\_DEM\_4 = DEMAND\_1\*IF(P\_CCR\_PROD\_START\_TIME>5 AND P\_CCR\_PROD\_START\_TIME<=6,1,0)  
doc DELAY\_DEM\_4 = This is the DEMAND whose production -in order to be dispatched on time- has P\_CCR\_PROD\_START\_TIME more than 5 and less than 6. The production of this demand has to start at the shop's CCR operation (i.e. it has to become part of the rate CCR\_PROD\_R) at the start of the 5th day after the current time interval. Therefore, it has to be added at the rate P\_CCR\_PROD\_R 4 days after the current time interval.  
unit DELAY\_DEM\_4 = ITEMS

aux DELAY\_DEM\_5 = DEMAND\_1\*IF(P\_CCR\_PROD\_START\_TIME>6 AND P\_CCR\_PROD\_START\_TIME<=7,1,0)  
doc DELAY\_DEM\_5 = This is the DEMAND whose production -in order to be dispatched on time- has P\_CCR\_PROD\_START\_TIME more than 6 and less than 7. The production of this demand has to start at the shop's CCR of the shop (i.e. it has to become part of the rate CCR\_PROD\_R) at the start of the 6th day after the current time interval. Therefore, it has to be added at the rate P\_CCR\_PROD\_R 5 days after the current time interval.  
unit DELAY\_DEM\_5 = ITEMS

aux DELAY\_DEM\_6 = DEMAND\_1\*IF(P\_CCR\_PROD\_START\_TIME>7 AND P\_CCR\_PROD\_START\_TIME<=8,1,0)

doc DELAY\_DEM\_6 = This is the DEMAND whose production -in order to be dispatched on time- has P\_CCR\_PROD\_START\_TIME more than 7 and less than 8. The production of this demand has to start at the shop's CCR operation (i.e. it has to become part of the rate CCR\_PROD\_R) at the start of the 7th day after the current time interval. Therefore, it has to be added at the rate P\_CCR\_PROD\_R 6 days after the current time interval.

unit DELAY\_DEM\_6 = ITEMS

aux DELAY\_DEM\_7 = DEMAND\_1\*IF(P\_CCR\_PROD\_START\_TIME>8,1,0)

doc DELAY\_DEM\_7 = This is the DEMAND whose production -in order to be dispatched on time- has P\_CCR\_PROD\_START\_TIME more than 8. The production of this demand has to start at the shop's CCR operation (i.e. it has to become part of the rate CCR\_PROD\_R) at the start of the 8th day after the current time interval. Therefore, it has to be added at the rate P\_CCR\_PROD\_R 7 days after the current time interval.

unit DELAY\_DEM\_7 = ITEMS

aux DELAY\_MAT\_3 = MAT\_ORDER\*IF(MAT\_L\_TIME=3,1,0)

doc DELAY\_MAT\_3 = This is the raw material order which fulfillment is planned to be 3 days after its release.

unit DELAY\_MAT\_3 = Kg

aux DELAY\_MAT\_4 = MAT\_ORDER\*IF(MAT\_L\_TIME>3 AND MAT\_L\_TIME<=4,1,0)

doc DELAY\_MAT\_4 = This is the raw material order which fulfillment is planned to be at the 4th day after its release.

unit DELAY\_MAT\_4 = Kg

aux DELAY\_MAT\_5 = MAT\_ORDER\*IF(MAT\_L\_TIME>4 AND MAT\_L\_TIME<=5,1,0)

doc DELAY\_MAT\_5 = This is the raw material order which fulfillment is planned to be at the 5th day after its release.

unit DELAY\_MAT\_5 = Kg

aux DELAY\_MAT\_6 = MAT\_ORDER\*IF(MAT\_L\_TIME>5,1,0)

doc DELAY\_MAT\_6 = This is the raw material order which fulfillment is planned to be at the 6th day after its release.

unit DELAY\_MAT\_6 = Kg

aux DEM\_SD = DEM\_M/4

doc DEM\_SD = This is the standard deviation of the demand for the case of the normally distributed demand. It is set equal to 1/4 of the demand mean (DEM\_M).

unit DEM\_SD = ITEMS/DAY

aux DEMAND = 1\*NORMAL(DEM\_M, DEM\_SD,0.1)+0\*PULSE(1000,400,10000)+0\*(7.5+SINWAVE(1.5,500))

doc DEMAND = This is the current demand of the shop. It follows a normal distribution with mean value and standard deviation equal to DEM\_M and

DEM\_SD respectively. In case we want to have a demand pulse or a wavy demand we change the required 0 to 1.

unit DEMAND = ITEMS/DAY

aux DEMAND\_1 = DEMAND\*TIMESTEP

doc DEMAND\_1 = This is the demand of the shop at the current time interval.

unit DEMAND\_1 = ITEMS

aux DIVERGENCE = ABS(P\_DEM\_FULF-SHIPMENTS)

doc DIVERGENCE = This is the absolute difference between the planned demand fulfillment and the actual shipments at the current time interval.

unit DIVERGENCE = ITEMS

aux MAT\_L\_TIME = RANDOM(P\_MAT\_L\_TIME,2\*P\_MAT\_L\_TIME,0.2)  
\*MAT\_ORDER\_SWITCH

doc MAT\_L\_TIME = This is the real value of the material lead time. It is uniformly distributed between the planned material lead time and the twofold value of it.

unit MAT\_L\_TIME = DAYS

aux MAT\_L\_TIME\_M = 1.5\*P\_MAT\_L\_TIME

doc MAT\_L\_TIME\_M = This is the mean value of the real material lead time for the raw material used.

unit MAT\_L\_TIME\_M = DAYS

aux MAT\_ORDER = IF(MAT\_ORDER\_ROPE>0,IF(MAT\_TIME\_BUFFER  
<MIN\_P\_MAT\_TIME\_BUFFER,MAT\_ORDER\_QUANTITY,0),0)

doc MAT\_ORDER = This is the raw material quantity we order at the current time interval. Its value is equal to zero whenever the CCR operation of the shop was idle at the time interval four timesteps before the current one. Otherwise, its value is equal to the material order quantity (MAT\_ORDER\_QUANTITY) whenever the current material time buffer is less than its minimum planned value.

unit MAT\_ORDER = Kg

aux MAT\_ORDER\_QUANTITY = 3\*P\_MAT\_L\_TIME\*MAT\_FACTOR  
/PROD\_DUR\_2\_M

doc MAT\_ORDER\_QUANTITY = This is the quantity of the material order batch. It is set equal to 3 times the raw material usage expected during the planned material lead time considering that the CCR machine operates at its capacity; i.e. it is equal to 3 times the material required to fulfill the average material demand of the CCR operation during the planned material lead time (P\_MAT\_L\_TIME).

unit MAT\_ORDER\_QUANTITY = Kg

aux MAT\_ORDER\_ROPE = DELAYPPL(PROD\_R\_2,4\*TIMESTEP,0)

doc MAT\_ORDER\_ROPE = This is the rope of the DBR logic for the raw material procurement process. We set this rope by using the Real Time (RT) methodology, i.e. the raw material inventory is monitored for material order at the rate at which the products are processed by the CCR operation of the shop and with a delay of 4 timesteps in order the size of timestep to fulfill the constraint:  $dt \leq T/2n$ .

unit MAT\_ORDER\_ROPE = ITEMS/DAY

aux MAT\_ORDER\_SWITCH = IF(MAT\_ORDER>0,1,0)

doc MAT\_ORDER\_SWITCH = This is a switch pointing that we order raw material at the current time interval.

aux MAT\_PROC\_3 = DELAYPPL(DELAY\_MAT\_3,3,0)

doc MAT\_PROC\_3 = This is the raw material order quantity which fulfillment is planned to be 3 days after the current interval, in order the material order part named DELAY\_MAT\_3 to be received on time.

unit MAT\_PROC\_3 = Kg

aux MAT\_PROC\_4 = DELAYPPL(DELAY\_MAT\_4,4,0)

doc MAT\_PROC\_4 = This is the raw material order quantity which fulfillment is planned to be at the 4th day after the current interval, in order the material order part named DELAY\_MAT\_4 to be received on time.

unit MAT\_PROC\_4 = Kg

aux MAT\_PROC\_5 = DELAYPPL(DELAY\_MAT\_5,5,0)

doc MAT\_PROC\_5 = This is the raw material order quantity which fulfillment is planned to be at the 5th day after the current interval, in order the material order part named DELAY\_MAT\_5 to be received on time.

unit MAT\_PROC\_5 = Kg

aux MAT\_PROC\_6 = DELAYPPL(DELAY\_MAT\_6,6,0)

doc MAT\_PROC\_6 = This is the raw material order quantity which fulfillment is planned to be at the 6th day after the current interval, in order the material order part named DELAY\_MAT\_6 to be received on time.

unit MAT\_PROC\_6 = Kg

aux MAT\_TIME\_BUFFER =  
(MATERIAL+MATERIAL\_IN\_TRANSIT)/MAT\_FACTOR\*PROD\_DUR\_2\_M

doc MAT\_TIME\_BUFFER = This is the current material time buffer of the material procurement process; i.e. it is the current material inventory on hand and in transit expressed in time units of the shop's CCR operation. This buffer is continually monitored in order to be more than the minimum planned material time buffer required (MIN\_P\_MAT\_TIME\_BUFFER). Whenever MAT\_TIME\_BUFFER is less than MIN\_P\_MAT\_TIME\_BUFFER we order a material order quantity (Q\_MAT\_QUANTITY).

unit MAT\_TIME\_BUFFER = DAYS

aux MIN\_P\_MAT\_TIME\_BUFFER =  
CEIL(3\*DEM\_M\*TIMESTEP\*MAT\_FACTOR/MAT\_ORDER\_QUANTITY)\*  
MAT\_L\_TIME\_M+3\*DEM\_M\*TIMESTEP\*PROD\_DUR\_1\_M

doc MIN\_P\_MAT\_TIME\_BUFFER = This is the minimum required material time buffer of the raw material procurement process. It is set equal to 3 times the mean value of duration before the CCR operation (i.e. for procurement of raw material and for production at operation 1) for the mean value of demand during one time

interval. Note that the number of material orders necessary to cover the respective material quantity is set equal to the smallest integer greater than or equal to its original estimated value.

unit MIN\_P\_MAT\_TIME\_BUFFER = DAYS

aux MIN\_P\_PR\_TIME\_BUFFER = 3\*DEM\_M\*TIMESTEP\*PROD\_DUR\_1\_M

doc MIN\_P\_PR\_TIME\_BUFFER = This is the minimum planned production time buffer which is required before the CCR operation. It is set equal to 3 times the mean value of production duration before the CCR operation (i.e. for operation 1) for the mean value of Demand during one time interval.

unit MIN\_P\_PR\_TIME\_BUFFER = DAYS

aux P\_CCR\_PR\_4 = DELAYPPL(DELAY\_DEM\_3,3,0)

doc P\_CCR\_PR\_4 = This is the production which is added to the rate P\_CCR\_PROD\_R at the 3rd day after the current interval, in order the demand part named DELAY\_DEM\_3 to be satisfied on time. Therefore, it is planned to start at the CCR operation of the shop at the start of the 4th day after the current interval.

unit P\_CCR\_PR\_4 = ITEMS

aux P\_CCR\_PR\_5 = DELAYPPL(DELAY\_DEM\_4,4,0)

doc P\_CCR\_PR\_5 = This is the production which is added to the rate P\_CCR\_PROD\_R at the 4th day after the current interval, in order the demand part named DELAY\_DEM\_4 to be satisfied on time. Therefore, it is planned to start at the CCR operation of the shop at the start of the 5th day after the current interval.

unit P\_CCR\_PR\_5 = ITEMS

aux P\_CCR\_PR\_6 = DELAYPPL(DELAY\_DEM\_5,5,0)

doc P\_CCR\_PR\_6 = This is the production which is added to the rate P\_CCR\_PROD\_R at the 5th day after the current interval, in order the demand part named DELAY\_DEM\_5 to be satisfied on time. Therefore, it is planned to start at the CCR operation of the shop at the start of the 6th day after the current interval.

unit P\_CCR\_PR\_6 = ITEMS

aux P\_CCR\_PR\_7 = DELAYPPL(DELAY\_DEM\_6,6,0)

doc P\_CCR\_PR\_7 = This is the production which is added to the rate P\_CCR\_PROD\_R at the 6th day after the current interval, in order the demand part named DELAY\_DEM\_6 to be satisfied on time. Therefore, it is planned to start at the CCR operation of the shop at the start of the 7th day after the current interval.

unit P\_CCR\_PR\_7 = ITEMS

aux P\_CCR\_PR\_8 = DELAYPPL(DELAY\_DEM\_7,7,0)

doc P\_CCR\_PR\_8 = This is the production which is added to the rate P\_CCR\_PROD\_R at the 7th day after the current interval, in order the demand part named DELAY\_DEM\_7 to be satisfied on time. Therefore, it is planned to

start at the CCR operation of the shop at the start of the 8th day after the current interval.

unit P\_CCR\_PR\_8 = ITEMS

aux P\_CCR\_PROD\_START\_TIME = MAX(0,P\_LEAD\_TIME-  
REQ\_PROD\_DURATION\_2\_3-MIN\_P\_PR\_TIME\_BUFFER)

doc P\_CCR\_PROD\_START\_TIME = This is the planned time available for the demand production at the shop's operations before the CCR one, in order the demand production at the CCR stage to start on time, i.e. the demand production is finished up to its planned lead time. The minimum production time buffer is subtracted by this time, in order to anticipate any possible delay to the average time of production duration in operations 2 and 3. If the calculated difference is negative, the demand production at the CCR operation of the shop has to be start immediately, because its fulfillment is expected later than the planned lead time.

unit P\_CCR\_PROD\_START\_TIME = DAYS

aux P\_DEM\_FULF = DELAYPPL(DEMAND\_1,P\_LEAD\_TIME,0)

doc P\_DEM\_FULF = This is the demand we have to satisfy at the current time interval. It is equal with the demand occurred 10 days ago, whereas 10 stands for the duration of the planned lead time (P\_LEAD\_TIME).

unit P\_DEM\_FULF = ITEMS

aux PR\_TIME\_BUFFER = WIP\_1\*PROD\_DUR\_2\_M

doc PR\_TIME\_BUFFER = This is the current time buffer before the CCR operation of the shop; i.e. it is the current WIP\_1 expressed in time units of the shop's CCR operation. This buffer is continually monitored in order to be more than the minimum planned production time buffer required (MIN\_P\_PR\_TIME\_BUFFER). Whenever PR\_TIME\_BUFFER is less than MIN\_P\_PR\_TIME\_BUFFER we produce at the first operation (i.e. before the CCR operation) with the maximum production rate possible considering the availability of raw material.

unit PR\_TIME\_BUFFER = DAYS

aux PROD\_DUR\_1 = EXPRND(PROD\_DUR\_1\_M,0.3)

doc PROD\_DUR\_1 = This is the production duration of the items processed at the gateway operation of the shop (operation 1) at the current time interval. This duration follows an exponential distribution with mean value equal to PROD\_DUR\_1\_M.

unit PROD\_DUR\_1 = DAYS/ITEM

aux PROD\_DUR\_2 = EXPRND(PROD\_DUR\_2\_M,0.4)

doc PROD\_DUR\_2 = This is the production duration of the items processed at the shop's CCR operation (operation 2) at the current time interval. This duration follows an exponential distribution with mean value equal to PROD\_DUR\_2\_M.

unit PROD\_DUR\_2 = DAYS/ITEM

aux PROD\_DUR\_3 = EXPRND(PROD\_DUR\_3\_M,0.5)

doc PROD\_DUR\_3 = This is the production duration of the items processed at the end operation of the shop (operation 3) at the current time interval. This duration follows an exponential distribution with mean value equal to PROD\_DUR\_3\_M.  
unit PROD\_DUR\_3 = DAYS/ITEM

aux PROD\_R\_ROPE = DELAYPPL(PROD\_R\_2,4\*TIMESTEP,0)  
doc PROD\_R\_ROPE = This is the rope of the DBR logic for the production process. We set this rope by using the Real Time (RT) methodology, i.e. raw material is released into the shop's gateway operation at the rate at which it is processed by the CCR and with a delay of 4 timesteps in order the size of timestep to fulfill the constraint:  $dt \leq T/2n$ .  
unit PROD\_R\_ROPE = ITEMS/DAY

aux REQ\_PROD\_DURATION\_2\_3 = (PROD\_DUR\_2\_M+1/(1/PROD\_DUR\_3\_M-DEM\_M))\*DEMAND\_1  
doc REQ\_PROD\_DURATION\_2\_3 = This is the mean expected time for the production of the demand of the current time interval from the CCR up to the end operation of the shop.  
unit REQ\_PROD\_DURATION\_2\_3 = DAYS

aux SHIPMENTS = SHIPMENTS\_R\*TIMESTEP  
doc SHIPMENTS = This is the demand satisfied at the current time interval.  
unit SHIPMENTS = ITEMS

const DEM\_M = 7.5  
doc DEM\_M = This is the mean value of the demand for the case of the normally distributed demand.  
unit DEM\_M = ITEMS/DAY

const MAT\_FACTOR = 2  
doc MAT\_FACTOR = This is the quantity of raw material required for the production of 1 item of the product.  
unit MAT\_FACTOR = Kg/ITEM

const P\_LEAD\_TIME = 10  
doc P\_LEAD\_TIME = This is the planned lead time, i.e. it is the duration available for the production of the demand from the time of the demand release up to the time of its planned fulfillment.  
unit P\_LEAD\_TIME = DAYS

const P\_MAT\_L\_TIME = 3  
doc P\_MAT\_L\_TIME = This is the planned material lead time for the raw material, that it is offered by the supplier.  
unit P\_MAT\_L\_TIME = DAYS

const PROD\_DUR\_1\_M = 0.0625  
doc PROD\_DUR\_1\_M = This is the mean value of the process duration at the gateway operation of the shop (operation 1).

unit PROD\_DUR\_1\_M = DAYS/ITEM

const PROD\_DUR\_2\_M = 0.125

doc PROD\_DUR\_2\_M = This is the mean value of the process duration at the shop's  
CCR operation (operation 2).

unit PROD\_DUR\_2\_M = DAYS/ITEM

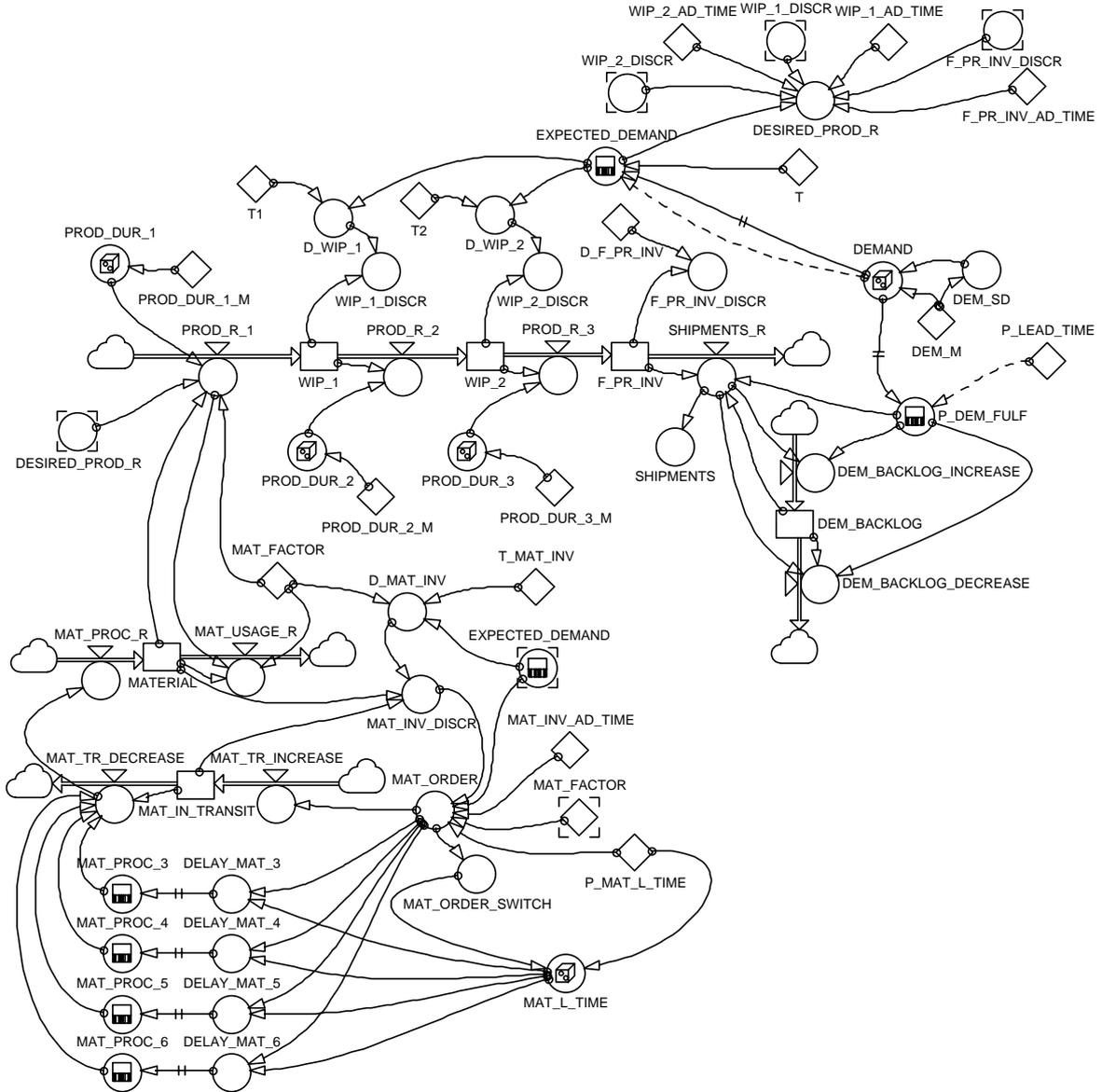
const PROD\_DUR\_3\_M = 0.0625

doc PROD\_DUR\_3\_M = This is the mean value of the process duration at the end  
operation of the shop (operation 3).

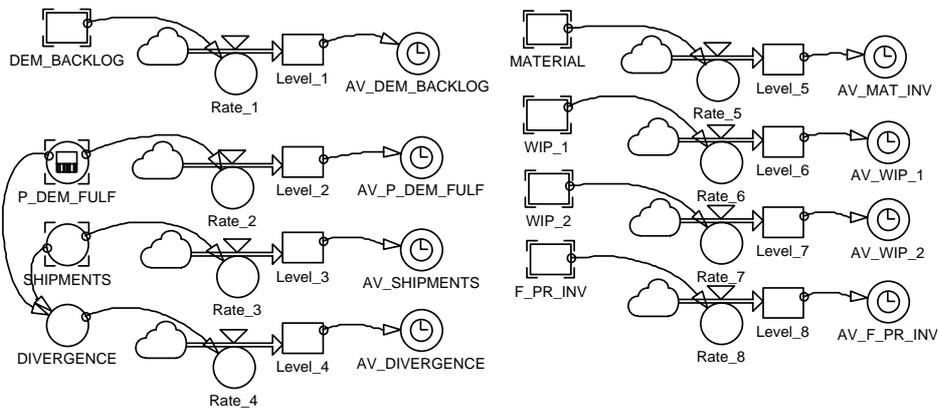
unit PROD\_DUR\_3\_M = DAYS/ITEM

## B. AA approach

### B.1 Stock-flow Diagram for Scheduling and Production Sector



### B.2 Stock-flow Diagram for Controlling Sector



### B.3 Equations

init DEM\_BACKLOG = 0  
flow DEM\_BACKLOG =  $-dt \cdot \text{DEM\_BACKLOG\_DECREASE}$   
 $+dt \cdot \text{DEM\_BACKLOG\_INCREASE}$   
doc DEM\_BACKLOG = This is the demand, whose fulfillment is going to be delayed  
(i.e. it is going to be satisfied more than 10 days after its release).  
unit DEM\_BACKLOG = ITEMS

init F\_PR\_INV = 0  
flow F\_PR\_INV =  $-dt \cdot \text{SHIPMENTS\_R} + dt \cdot \text{PROD\_R\_3}$   
doc F\_PR\_INV = This is the inventory of the finished product, which is available after  
the end operation of the shop.  
unit F\_PR\_INV = ITEMS

init Level\_1 = 0  
flow Level\_1 =  $+dt \cdot \text{Rate}_1$   
doc Level\_1 = This level is used to calculate the average value of the demand backlog  
(AV\_DEM\_BACKLOG).  
unit Level\_1 = ITEMS\*days

init Level\_2 = 0  
flow Level\_2 =  $+dt \cdot \text{Rate}_2$   
doc Level\_2 = This level is used to calculate the average value of the planned demand  
fulfillment (AV\_P\_DEM\_FULF).  
unit Level\_2 = ITEMS

init Level\_3 = 0  
flow Level\_3 =  $+dt \cdot \text{Rate}_3$   
doc Level\_3 = This level is used to calculate the average value of the shipments  
(AV\_SHIPMENTS).  
unit Level\_3 = ITEMS

init Level\_4 = 0  
flow Level\_4 =  $+dt \cdot \text{Rate}_4$   
doc Level\_4 = This level is used to calculate the average value of the divergence  
(AV\_DIVERGENCE).  
unit Level\_4 = ITEMS

init Level\_5 = 0  
flow Level\_5 =  $+dt \cdot \text{Rate}_5$   
doc Level\_5 = This level is used to calculate the average value of the raw material  
inventory (AV\_MAT\_INV).  
unit Level\_5 = Kg\*days

init Level\_6 = 0  
flow Level\_6 =  $+dt \cdot \text{Rate}_6$   
doc Level\_6 = This level is used to calculate the average value of the inventory after  
the first operation of the flow shop (AV\_WIP\_1).

unit Level\_6 = ITEMS\*DAYS

init Level\_7 = 0

flow Level\_7 = +dt\*Rate\_7

doc Level\_7 = This level is used to calculate the average value of the inventory after the second operation of the flow shop (AV\_WIP\_2).

unit Level\_7 = ITEMS\*DAYS

init Level\_8 = 0

flow Level\_8 = +dt\*Rate\_8

doc Level\_8 = This level is used to calculate the average value of the finished product inventory of the flow shop (AV\_F\_PR\_INV).

unit Level\_8 = ITEMS\*DAYS

init MAT\_IN\_TRANSIT = 0

flow MAT\_IN\_TRANSIT = -dt\*MAT\_TR\_DECREASE+dt\*MAT\_TR\_INCREASE

doc MAT\_IN\_TRANSIT = This is the current level of material inventory in transit; i.e. the material inventory that has been ordered and it is expected to be delivered at the shop later. Its initial value is set equal to zero.

unit MAT\_IN\_TRANSIT = Kg

init MATERIAL = 2\*144

flow MATERIAL = -dt\*MAT\_USAGE\_R+dt\*MAT\_PROC\_R

doc MATERIAL = This is the current level of raw material inventory on hand.

unit MATERIAL = Kg

init WIP\_1 = 0

flow WIP\_1 = +dt\*PROD\_R\_1-dt\*PROD\_R\_2

doc WIP\_1 = This is the inventory available before the shop's CCR operation.

unit WIP\_1 = ITEMS

init WIP\_2 = 0

flow WIP\_2 = -dt\*PROD\_R\_3+dt\*PROD\_R\_2

doc WIP\_2 = This is the inventory available after the shop's CCR operation.

unit WIP\_2 = ITEMS

aux DEM\_BACKLOG\_DECREASE = MIN(MAX(SHIPMENTS\_R-P\_DEM\_FULF/TIMESTEP,0),DEM\_BACKLOG/TIMESTEP)

doc DEM\_BACKLOG\_DECREASE = This is the demand fulfillment with delay at the current time interval; i.e. it is the demand satisfied later than 10 days (LEAD\_TIME) after its release.

unit DEM\_BACKLOG\_DECREASE = ITEMS/DAY

aux DEM\_BACKLOG\_INCREASE = MAX(P\_DEM\_FULF/TIMESTEP-SHIPMENTS\_R,0)

doc DEM\_BACKLOG\_INCREASE = This is the invalid demand fulfillment at the current time interval; i.e. it is the demand that although has to be satisfied at the

current time interval (10 days after its release), it is impossible to be satisfied on time.

unit DEM\_BACKLOG\_INCREASE = ITEMS/DAY

aux MAT\_PROC\_R = MAT\_TR\_DECREASE

doc MAT\_PROC\_R = This is the rate of the raw material procurement received; i.e. the raw material delivery at the current time interval. It is set equal to the material in transit decrease.

unit MAT\_PROC\_R = kg/DAY

aux MAT\_TR\_DECREASE = MIN(MAT\_PROC\_3+MAT\_PROC\_4+MAT\_PROC\_5+MAT\_PROC\_6,MAT\_IN\_TRANSIT)/TIMESTEP

doc MAT\_TR\_DECREASE = This is the rate of the raw material received; i.e. the raw material delivery at the current time interval.

unit MAT\_TR\_DECREASE = kg/DAY

aux MAT\_TR\_INCREASE = MAT\_ORDER/TIMESTEP

doc MAT\_TR\_INCREASE = This is the raw material quantity ordered at the current time interval.

unit MAT\_TR\_INCREASE = kg/DAY

aux MAT\_USAGE\_R = MIN(PROD\_R\_1\*MAT\_FACTOR, MATERIAL/TIMESTEP)

doc MAT\_USAGE\_R = This is the rate of the raw material usage by the production at the gateway operation of the shop (PROD\_R\_1).

unit MAT\_USAGE\_R = kg/DAY

aux PROD\_R\_1 = MIN(DESIRED\_PROD\_R,1/PROD\_DUR\_1, MATERIAL/MAT\_FACTOR/TIMESTEP)

doc PROD\_R\_1 = This is what we produce at the gateway operation of the shop according to the AA approach.

unit PROD\_R\_1 = ITEMS/DAY

aux PROD\_R\_2 = MIN(1/PROD\_DUR\_2,WIP\_1/TIMESTEP)

doc PROD\_R\_2 = This is what we produce at the shop's CCR operation.

unit PROD\_R\_2 = ITEMS/DAY

aux PROD\_R\_3 = MIN(1/PROD\_DUR\_3,WIP\_2/TIMESTEP)

doc PROD\_R\_3 = This is what we produce at the third operation of the shop.

unit PROD\_R\_3 = ITEMS/DAY

aux Rate\_1 = DEM\_BACKLOG

doc Rate\_1 = This rate is used to calculate the average value of the demand backlog (AV\_DEM\_BACKLOG).

unit Rate\_1 = ITEMS

aux Rate\_2 = P\_DEM\_FULF/TIMESTEP

doc Rate\_2 = This rate is used to calculate the average value of the planned demand fulfillment (AV\_P\_DEM\_FULF).  
unit Rate\_2 = ITEMS/DAY

aux Rate\_3 = SHIPMENTS/TIMESTEP  
doc Rate\_3 = This rate is used to calculate the average value of the shipments (AV\_SHIPMENTS).  
unit Rate\_3 = ITEMS/DAY

aux Rate\_4 = DIVERGENCE/TIMESTEP  
doc Rate\_4 = This rate is used to calculate the average value of the divergence (AV\_DIVERGENCE).  
unit Rate\_4 = ITEMS/DAY

aux Rate\_5 = MATERIAL  
doc Rate\_5 = This rate is used to calculate the average value of the raw material inventory (AV\_MAT\_INV).  
unit Rate\_5 = Kg

aux Rate\_6 = WIP\_1  
doc Rate\_6 = This rate is used to calculate the average value of the inventory after the first operation of the flow shop (AV\_WIP\_1).  
unit Rate\_6 = ITEMS

aux Rate\_7 = WIP\_2  
doc Rate\_7 = This rate is used to calculate the average value of the inventory after the second operation of the flow shop (AV\_WIP\_2).  
unit Rate\_7 = ITEMS

aux Rate\_8 = F\_PR\_INV  
doc Rate\_8 = This rate is used to calculate the average value of the finished product inventory of the flow shop (AV\_F\_PR\_INV).  
unit Rate\_8 = ITEMS

aux SHIPMENTS\_R = MIN(P\_DEM\_FULF+DEM\_BACKLOG,F\_PR\_INV) /TIMESTEP  
doc SHIPMENTS\_R = This is the rate of demand shipments.  
unit SHIPMENTS\_R = ITEMS/DAY

aux AV\_DEM\_BACKLOG = Level\_1 DIVZ0 TIME  
doc AV\_DEM\_BACKLOG = This is the average value of the demand backlog (DEM\_BACKLOG) from the simulation start up to the current time interval.  
unit AV\_DEM\_BACKLOG = ITEMS

aux AV\_DIVERGENCE = Level\_4 DIVZ0 TIME  
doc AV\_DIVERGENCE = This is the average value of the DIVERGENCE from the simulation start up to the current time interval.  
unit AV\_DIVERGENCE = ITEMS/DAY

aux AV\_F\_PR\_INV = Level\_8 DIVZ0 TIME  
 doc AV\_F\_PR\_INV = This is the average value of the finished product inventory (F\_PR\_INV) from the simulation start up to the current time interval.  
 unit AV\_F\_PR\_INV = ITEMS

aux AV\_MAT\_INV = Level\_5 DIVZ0 TIME  
 doc AV\_MAT\_INV = This is the average value of the raw material inventory on hand (MAT\_INV) from the simulation start up to the current time interval.  
 unit AV\_MAT\_INV = Kg

aux AV\_P\_DEM\_FULF = Level\_2 DIVZ0 TIME  
 doc AV\_P\_DEM\_FULF = This is the average value of the planned demand fulfillment (P\_DEM\_FULF) from the simulation start up to the current time interval.  
 unit AV\_P\_DEM\_FULF = ITEMS/DAY

aux AV\_SHIPMENTS = Level\_3 DIVZ0 TIME  
 doc AV\_SHIPMENTS = This is the average value of the SHIPMENTS from the simulation start up to the current time interval.  
 unit AV\_SHIPMENTS = ITEMS/DAY

aux AV\_WIP\_1 = Level\_6 DIVZ0 TIME  
 doc AV\_WIP\_1 = This is the average value of the inventory after the first operation of the shop (WIP\_1) from the simulation start up to the current time interval.  
 unit AV\_WIP\_1 = ITEMS

aux AV\_WIP\_2 = Level\_7 DIVZ0 TIME  
 doc AV\_WIP\_2 = This is the average value of the inventory after the second operation of the shop (WIP\_2) from the simulation start up to the current time interval.  
 unit AV\_WIP\_2 = ITEMS

aux D\_MAT\_INV = T\_MAT\_INV\*EXPECTED\_DEMAND\*MAT\_FACTOR  
 doc D\_MAT\_INV = This is the desired raw material inventory according to the AA approach.  
 unit D\_MAT\_INV = Kg

aux D\_WIP\_1 = T1\*EXPECTED\_DEMAND  
 doc D\_WIP\_1 = This is the desired inventory after the first operation of the shop according to the AA approach.  
 unit D\_WIP\_1 = ITEMS

aux D\_WIP\_2 = T2\*EXPECTED\_DEMAND  
 doc D\_WIP\_2 = This is the desired inventory after the second operation of the shop according to the AA approach.  
 unit D\_WIP\_2 = ITEMS

aux DELAY\_MAT\_3 = MAT\_ORDER\*IF(MAT\_L\_TIME=3,1,0)

doc DELAY\_MAT\_3 = This is the raw material order which delivery is planned to be 3 days after its release.

unit DELAY\_MAT\_3 = Kg

aux DELAY\_MAT\_4 = MAT\_ORDER\*IF(MAT\_L\_TIME>3 AND MAT\_L\_TIME<=4,1,0)

doc DELAY\_MAT\_4 = This is the raw material order which delivery is planned to be at the 4th day after its release.

unit DELAY\_MAT\_4 = Kg

aux DELAY\_MAT\_5 = MAT\_ORDER\*IF(MAT\_L\_TIME>4 AND MAT\_L\_TIME<=5,1,0)

doc DELAY\_MAT\_5 = This is the raw material order which delivery is planned to be at the 5th day after its release.

unit DELAY\_MAT\_5 = Kg

aux DELAY\_MAT\_6 = MAT\_ORDER\*IF(MAT\_L\_TIME>5,1,0)

doc DELAY\_MAT\_6 = This is the raw material order which delivery is planned to be at the 6th day after its release.

unit DELAY\_MAT\_6 = Kg

aux DEM\_SD = DEM\_M/4

doc DEM\_SD = This is the standard deviation of the demand for the case of the normally distributed demand. It is set equal to 1/4 of the demand mean (DEM\_M).

unit DEM\_SD = ITEMS/DAY

aux DEMAND = 1\*NORMAL(DEM\_M,DEM\_SD,0.1)+0\*PULSE(1000,400,10000)+0\*(7.5+SINWAVE(1.5,500))

doc DEMAND = This is the current demand of the shop. It follows a normal distribution with mean value and standard deviation equal to DEM\_M and DEM\_SD respectively. In case we want to have a demand pulse or a wavy demand we change the required 0 to 1.

unit DEMAND = ITEMS/DAY

aux DESIRED\_PROD\_R = MAX(0,EXPECTED\_DEMAND +F\_PR\_INV\_DISCR/F\_PR\_INV\_AD\_TIME+WIP\_2\_DISCR/WIP\_2\_AD\_TIME +WIP\_1\_DISCR/WIP\_1\_AD\_TIME)

doc DESIRED\_PROD\_R = This is the desired production rate of the first operation of the shop according to the AA approach.

unit DESIRED\_PROD\_R = ITEMS/DAY

aux DIVERGENCE = ABS(P\_DEM\_FULF-SHIPMENTS)

doc DIVERGENCE = This is the absolute difference between the planned demand fulfillment and the actual shipments at the current time interval.

unit DIVERGENCE = ITEMS/DAY

aux EXPECTED\_DEMAND = DELAYINF(DEMAND,T,1,DEMAND)

doc EXPECTED\_DEMAND = This is the demand expected to occur at the current day of simulation according to the AA approach.

unit EXPECTED\_DEMAND = ITEMS/DAY

aux F\_PR\_INV\_DISCR = D\_F\_PR\_INV-F\_PR\_INV

doc F\_PR\_INV\_DISCR = This is the discrepancy occurred at the current time interval between the desired finished product inventory and its real value.

unit F\_PR\_INV\_DISCR = ITEMS

aux MAT\_INV\_DISCR = D\_MAT\_INV-MATERIAL-MAT\_IN\_TRANSIT

doc MAT\_INV\_DISCR = This is the discrepancy occurred at the current time interval between the desired raw material inventory and its real value.

unit MAT\_INV\_DISCR = Kg

aux MAT\_L\_TIME = RANDOM(P\_MAT\_L\_TIME,2\*P\_MAT\_L\_TIME,0.2)  
\*MAT\_ORDER\_SWITCH

doc MAT\_L\_TIME = This is the real value of the raw material lead time. It is uniformly distributed between the planned material lead time and the twofold value of it.

unit MAT\_L\_TIME = DAYS

aux MAT\_ORDER = MAX(0,MAT\_INV\_DISCR/MAT\_INV\_AD\_TIME  
\*TIMESTEP+EXPECTED\_DEMAND\*P\_MAT\_L\_TIME\*MAT\_FACTOR)

doc MAT\_ORDER = This is the raw material quantity we order at the current time interval according to the AA approach.

unit MAT\_ORDER = Kg

aux MAT\_ORDER\_SWITCH = IF(MAT\_ORDER>0,1,0)

doc MAT\_ORDER\_SWITCH = This is a switch pointing that we order raw material at the current time interval.

aux MAT\_PROC\_3 = DELAYPPL(DELAY\_MAT\_3,3,0)

doc MAT\_PROC\_3 = This is the raw material order quantity which delivery is planned to be 3 days after the current interval, in order the material order part named DELAY\_MAT\_3 to be received on time.

unit MAT\_PROC\_3 = Kg

aux MAT\_PROC\_4 = DELAYPPL(DELAY\_MAT\_4,4,0)

doc MAT\_PROC\_4 = This is the raw material order quantity which delivery is planned to be at the 4th day after the current interval, in order the material order part named DELAY\_MAT\_4 to be received on time.

unit MAT\_PROC\_4 = Kg

aux MAT\_PROC\_5 = DELAYPPL(DELAY\_MAT\_5,5,0)

doc MAT\_PROC\_5 = This is the raw material order quantity which delivery is planned to be at the 5th day after the current interval, in order the material order part named DELAY\_MAT\_5 to be received on time.

unit MAT\_PROC\_5 = Kg

aux  $\text{MAT\_PROC\_6} = \text{DELAYPPL}(\text{DELAY\_MAT\_6}, 6, 0)$   
 doc  $\text{MAT\_PROC\_6}$  = This is the raw material order quantity which delivery is planned to be at the 6th day after the current interval, in order the material order part named  $\text{DELAY\_MAT\_6}$  to be received on time.  
 unit  $\text{MAT\_PROC\_6} = \text{Kg}$

aux  $\text{P\_DEM\_FULF} = \text{DELAYPPL}(\text{DEMAND}, \text{P\_LEAD\_TIME}, 0) * \text{TIMESTEP}$   
 doc  $\text{P\_DEM\_FULF}$  = This is the demand we have to satisfy at the current time interval. It is equal with the demand occurred 10 days ago, whereas 10 stands for the duration of the planned lead time ( $\text{P\_LEAD\_TIME}$ ).  
 unit  $\text{P\_DEM\_FULF} = \text{ITEMS}$

aux  $\text{PROD\_DUR\_1} = \text{EXPRND}(\text{PROD\_DUR\_1\_M}, 0.3)$   
 doc  $\text{PROD\_DUR\_1}$  = This is the production duration of the items processed at the gateway operation of the shop (operation 1) at the current time interval. This duration follows an exponential distribution with mean value equal to  $\text{PROD\_DUR\_1\_M}$ .  
 unit  $\text{PROD\_DUR\_1} = \text{DAYS/ITEM}$

aux  $\text{PROD\_DUR\_2} = \text{EXPRND}(\text{PROD\_DUR\_2\_M}, 0.4)$   
 doc  $\text{PROD\_DUR\_2}$  = This is the production duration of the items processed at the CCR operation of the shop (operation 2) at the current time interval. This duration follows an exponential distribution with mean value equal to  $\text{PROD\_DUR\_2\_M}$ .  
 unit  $\text{PROD\_DUR\_2} = \text{DAYS/ITEM}$

aux  $\text{PROD\_DUR\_3} = \text{EXPRND}(\text{PROD\_DUR\_3\_M}, 0.5)$   
 doc  $\text{PROD\_DUR\_3}$  = This is the production duration of the items processed at the end operation of the shop (operation 3) at the current time interval. This duration follows an exponential distribution with mean value equal to  $\text{PROD\_DUR\_3\_M}$ .  
 unit  $\text{PROD\_DUR\_3} = \text{DAYS/ITEM}$

aux  $\text{SHIPMENTS} = \text{SHIPMENTS\_R} * \text{TIMESTEP}$   
 doc  $\text{SHIPMENTS}$  = This is the demand we satisfy at the current time interval.  
 unit  $\text{SHIPMENTS} = \text{ITEMS}$

aux  $\text{WIP\_1\_DISCR} = \text{D\_WIP\_1} - \text{WIP\_1}$   
 doc  $\text{WIP\_1\_DISCR}$  = This is the discrepancy occurred at the current time interval between the desired inventory after the operation 1 of the shop and its real value.  
 unit  $\text{WIP\_1\_DISCR} = \text{ITEMS}$

aux  $\text{WIP\_2\_DISCR} = \text{D\_WIP\_2} - \text{WIP\_2}$   
 doc  $\text{WIP\_2\_DISCR}$  = This is the discrepancy occurred at the current time interval between the desired inventory after the shop's CCR operation (operation 2) and its real value.  
 unit  $\text{WIP\_2\_DISCR} = \text{ITEMS}$

const  $\text{D\_F\_PR\_INV} = 0$

doc D\_F\_PR\_INV = This is the desired finished product inventory of the shop according to the AA approach.  
unit D\_F\_PR\_INV = ITEMS

const DEM\_M = 7.5  
doc DEM\_M = This is the mean value of the demand for the case of the normally distributed demand.  
unit DEM\_M = ITEMS/DAY

const F\_PR\_INV\_AD\_TIME = 2  
doc F\_PR\_INV\_AD\_TIME = This is the adjustment time for the finished products inventory according to the AA approach. In case of scenario A it is set equal to 5, whereas in case of scenario B it is equal to 2.  
unit F\_PR\_INV\_AD\_TIME = DAYS

const MAT\_FACTOR = 2  
doc MAT\_FACTOR = This is the quantity of raw material required for the production of 1 item of the product.  
unit MAT\_FACTOR = Kg/ITEM

const MAT\_INV\_AD\_TIME = 2  
doc MAT\_INV\_AD\_TIME = This is the adjustment time for the raw material inventory according to the AA approach. In case of scenario A it is set equal to 5, whereas in case of scenario B it is equal to 2.  
unit MAT\_INV\_AD\_TIME = DAYS

const P\_LEAD\_TIME = 10  
doc P\_LEAD\_TIME = This is the planned lead time, i.e. it is the duration available for the production of the demand from the time of the demand release up to the time of its planned fulfillment.  
unit P\_LEAD\_TIME = DAYS

const P\_MAT\_L\_TIME = 3  
doc P\_MAT\_L\_TIME = This is the planned materials delivery lead time for the raw material, that it is offered by the supplier.  
unit P\_MAT\_L\_TIME = DAYS

const PROD\_DUR\_1\_M = 0.0625  
doc PROD\_DUR\_1\_M = This is the mean value of the process duration at the gateway operation of the shop (operation 1).  
unit PROD\_DUR\_1\_M = DAYS/ITEM

const PROD\_DUR\_2\_M = 0.125  
doc PROD\_DUR\_2\_M = This is the mean value of the process duration at the shop's CCR operation (operation 2).  
unit PROD\_DUR\_2\_M = DAYS/ITEM

const PROD\_DUR\_3\_M = 0.0625

doc PROD\_DUR\_3\_M = This is the mean value of the process duration at the end operation of the shop (operation 3).

unit PROD\_DUR\_3\_M = DAYS/ITEM

const T = 1

doc T = This is the time parameter used to calculate the expected demand according to the AA approach. In the case of the normally distributed demand it is equal to 23 days and in the case of the wavy demand it is equal to 1 day.

unit T = DAYS

const T\_MAT\_INV = 5

doc T\_MAT\_INV = This is the time parameter used to estimate the desired raw material inventory according to the AA approach. In case of scenario A it is set equal to 2, whereas in case of scenario B it is equal to 5.

unit T\_MAT\_INV = DAYS

const T1 = 5

doc T1 = This is the time parameter used to estimate the desired inventory after the first operation of the shop according to the AA approach. In case of scenario A it is set equal to 2, whereas in case of scenario B it is equal to 5.

unit T1 = DAYS

const T2 = 5

doc T2 = This is the time parameter used to estimate the desired inventory after the second operation of the shop according to the AA approach. In case of scenario A it is set equal to 2, whereas in case of scenario B it is equal to 5.

unit T2 = DAYS

const WIP\_1\_AD\_TIME = 2

doc WIP\_1\_AD\_TIME = This is the adjustment time for the inventory after the first operation of the shop according to the AA approach. In case of scenario A it is set equal to 5, whereas in case of scenario B it is equal to 2.

unit WIP\_1\_AD\_TIME = DAYS

const WIP\_2\_AD\_TIME = 2

doc WIP\_2\_AD\_TIME = This is the adjustment time for the inventory after the second operation of the shop according to the AA approach. In case of scenario A it is set equal to 5, whereas in case of scenario B it is equal to 2.

unit WIP\_2\_AD\_TIME = DAYS